

课后题

2022年6月16日 星期四 上午11:33

1. $2 \times 10^{-6} F$

1) $j = \frac{\partial D}{\partial t} = \epsilon \frac{\partial E}{\partial t} = \epsilon \frac{\partial V}{\partial t}$
 $I_d = jS = \frac{\epsilon S}{d} \frac{\partial V}{\partial t} = C \frac{dV}{dt}$

2) $I = \frac{V}{R} = I_d = C \frac{dV}{dt}$
 $\frac{dV}{dt} = \frac{V}{RC} \Rightarrow \ln V = \frac{t}{RC} + \ln C_1$

3) $\oint \vec{H} \cdot d\vec{l} = \int \vec{j} \cdot d\vec{S}$
 $B = \frac{\mu_0}{2\pi r} I_d = \frac{\mu_0}{2\pi r} j dS$
 $\int \vec{r} \times \vec{B} = \mu_0 \int I_d \vec{r} \times \frac{\vec{r}}{r} = \mu_0 \frac{r^2}{2} \left(C \frac{dV}{dt} \right) \Rightarrow \frac{dV}{dt} = \frac{2}{\mu_0 r^2} \int \vec{r} \times \vec{B}$

2. 1) $I = I_0 \cos \omega t, \vec{j} = j_0 \cos \omega t$
 $\vec{j}_D = \epsilon \frac{\partial \vec{E}}{\partial t} = \epsilon \frac{\partial}{\partial t} \left(\frac{j_0 \cos \omega t}{\sigma} \right) = \frac{\epsilon j_0 \omega \sin \omega t}{\sigma}$
 $\frac{j}{j_D} = \frac{\sigma j_0 \cos \omega t}{\epsilon \sigma j_0 \omega \sin \omega t} = \frac{\cot \omega t}{\epsilon \omega} = \frac{1}{\epsilon \omega}$

2) $\eta_1 = \frac{4\pi \times 10^{-7} \times \sigma}{\epsilon_0 \times 3.14 \times 10^9 \times 2 \times 10^{-5}}$
 $\eta_2 = \frac{4\pi \times 10^{-7} \times \sigma}{\epsilon_0 \times 3.14 \times 10^9 \times 2 \times 10^{-11}}$
 $T = \frac{1}{\omega}$
 $\omega = 2\pi f$

3. $B \times 2\pi r = \mu_0 \int (\vec{j} + \vec{j}_D) \cdot d\vec{S}$
 $= \mu_0 \frac{\pi r^2}{\pi a^2} \left(\frac{\partial Q}{\partial t} + \frac{\partial P}{\partial t} \right)$
 $\frac{\partial E}{\partial t} = \frac{1}{d} \frac{\partial V}{\partial t} = \mu_0 \frac{r^2}{a^2} \left(\omega Q_0 \cos \omega t + \epsilon_0 \frac{\partial E}{\partial t} \right)$
 $= \frac{1}{cd} \frac{\partial Q}{\partial t} = \mu_0 \frac{r^2}{a^2} \omega Q_0 \cos \omega t \left(1 + \frac{\epsilon}{cd} \right)$
 \vec{B} 与 \vec{E} 同相. $H = \frac{r}{2\pi r} \omega Q_0 \cos \omega t \left(1 + \frac{\epsilon}{cd} \right)$

4. $E_{r1} = E_{r2}, H_{\theta 1} = H_{\theta 2}$
 $\epsilon_1 E_{r1} = \epsilon_2 E_{r2}, \mu_1 H_{\theta 1} = \mu_2 H_{\theta 2}$
 $\Rightarrow E_1 \sin \theta_1 = E_2 \sin \theta_2, H_1 \sin \phi_1 = H_2 \sin \phi_2$
 $\epsilon_1 E_1 \sin \theta_1 = \epsilon_2 E_2 \sin \theta_2, \mu_1 H_1 \sin \phi_1 = \mu_2 H_2 \sin \phi_2$
 $\therefore \epsilon_1 \cos \theta_1 = \epsilon_2 \cos \theta_2, \mu_1 \cos \phi_1 = \mu_2 \cos \phi_2$

5. 1) $v = \frac{c}{\sqrt{\epsilon \mu}} = \frac{3 \times 10^8 \text{ m/s}}{\sqrt{2.53}} = \frac{3 \times 10^8}{1.6} \text{ m/s}$
 2) $T = \frac{1}{f}, \lambda = vT = \frac{v}{f}$
 3) $H = \sqrt{\frac{\epsilon}{\mu}} E$
 6. 1) $H = \sqrt{\frac{\epsilon}{\mu}} E$
 2) $f = 7.94 \times 10^7 \text{ Hz}$
 $\omega = 2\pi f, c = \frac{\omega}{k} = \frac{\omega}{k}$
 $k = \frac{\omega}{c} = \frac{2\pi \times 7.94 \times 10^7}{3 \times 10^8} = \frac{2\pi}{3.75}$
 3) $\lambda = \frac{2\pi}{k} = \frac{3.75 \times 10^8}{2\pi}$
 4) $\vec{S} = \frac{1}{\epsilon_0} \vec{E} \times \vec{B} = \frac{1}{\epsilon_0} \vec{E} \times \vec{H}$
 $P = \vec{S} \cdot 4\pi \vec{r}$

1. $C = 2 \times 10^{-6} F$
 $\vec{j}_D = \frac{\partial D}{\partial t}$
 $I_d = \int \frac{\partial \vec{D}}{\partial t} \cdot d\vec{S} = \epsilon_0 \int \frac{\partial \vec{E}}{\partial t} \cdot d\vec{S}$
 $C = \frac{4\pi \epsilon_0 S}{d} = \epsilon_0 \frac{4\pi \epsilon_0 S}{C} \frac{dV}{dt}$
 $d = \frac{C}{4\pi \epsilon_0 S}$
 $E = \frac{V}{d} = \frac{4\pi \epsilon_0 S V}{C}$
 $\vec{j} = \sigma \vec{E}, I = \frac{V}{R} = C \frac{dV}{dt}$
 $\frac{dC}{C} = \frac{1}{V} dV$
 $\int \frac{dC}{C} = \int \frac{1}{V} dV$
 $\ln C = \ln V + \ln C_1$
 $C = C_1 V$
 $\frac{dC}{C} = \frac{dV}{V}$
 $\int \frac{dC}{C} = \int \frac{dV}{V} \Rightarrow \ln C = \ln V + \ln C_1$
 $C = C_1 V$
 $\frac{dC}{C} = \frac{dV}{V}$
 $\int \frac{dC}{C} = \int \frac{dV}{V} \Rightarrow \ln C = \ln V + \ln C_1$
 $C = C_1 V$

5. $v = \frac{1}{\sqrt{\epsilon \mu}} = \frac{c}{\sqrt{2.53}}$
 $\lambda = vT = \frac{v}{f}$
 $H = \sqrt{\frac{\epsilon}{\mu}} E$

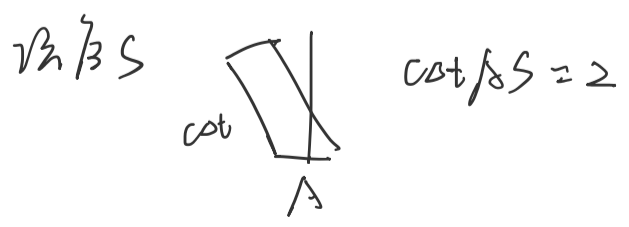
6. $H = \sqrt{\frac{\epsilon}{\mu}} E$
 $\lambda = \frac{v}{f} = \frac{\omega}{k}, k = \frac{\omega}{\lambda}, k = \frac{\omega}{c}$
 $\lambda = \frac{2\pi}{k}$

7. $P = 4\pi R^2 \vec{E} \cdot \vec{H}$
 $P = \frac{R^2 \sqrt{\epsilon}}{4\pi R^2} \int \vec{S} \cdot \vec{r} = \frac{1}{2} \vec{E} \times \vec{H} \cdot \vec{r}$

7. $\vec{E} = \vec{j} P = \frac{I P}{\pi a^2}$
 $\oint \vec{H} \cdot d\vec{l} = \frac{I}{2\pi r} \times 2\pi r = I \frac{r}{a^2}$
 $H \times 2\pi r = I \frac{r}{a^2}, H = \frac{I r}{2\pi a^2}$
 $\vec{S} = \vec{E} \times \vec{H} = -\frac{r I^2 P}{2\pi^2 a^4} \vec{e}_\theta$
 $P = \frac{I^2 V}{\sigma}, P = 2U = j S E l = \frac{I^2}{\sigma} 2\pi^2 l$

7. $\vec{E} = \frac{I}{\sigma} = \vec{j} P = \frac{I P}{\pi r^2}, r < a$
 $\vec{H} = \int \vec{j} \cdot d\vec{S} = \frac{I}{\pi a^2} \times \pi r^2 = \frac{I r}{a^2}, r < a$
 $\vec{S} = \frac{1}{2} \vec{E} \times \vec{H} = \frac{1}{2} \frac{I^2 P}{\pi^2 a^4} \vec{e}_\theta$
 $P = I U = I \times \frac{I P}{\pi r^2} l = \frac{I^2 P l}{\pi r^2} \times \left(\frac{1}{\pi a^2} \right)^2 \pi r^2 l P$
 从边界进入内部的电流

8. 1) $\vec{S} = 1353 \text{ W} \cdot \text{m}^{-2}$
 $\vec{P} = \vec{S} \cdot \vec{A} = S \times 4\pi d^2 = 1353 \times 4\pi \times (1.5 \times 10^{-1})^2$
 $\vec{S} = \frac{\vec{P}}{\vec{A}_0} = \frac{1353 \times 4\pi \times (1.5 \times 10^{-1})^2}{4\pi \times (1.7 \times 10^8)^2} = \frac{1353 \times 2.25}{49} \times 10^6$
 2) $\vec{S} = \frac{1}{2} \vec{E} \times \vec{H} = \frac{1}{2} \sqrt{\frac{\epsilon}{\mu}} E^2 = \frac{1}{2} c \epsilon_0 E^2$
 $E = \sqrt{\frac{2S}{c \epsilon_0}} = \sqrt{\frac{1353 \times 2.25 \times 10^6}{3 \times 10^8 \times 8.85 \times 10^{-12}}}$
 3) $H = \sqrt{\frac{\epsilon}{\mu}} E$



9. $S \cos \theta = P \cdot \cos \theta$
 $m v = F \cos \theta = P \cos \theta \Delta t$
 $F \cos \theta = \frac{2SA \cos \theta}{c}$
 $F \cos \theta = \frac{2SA \cos \theta}{c}$

10. $\vec{D} = \frac{Q}{4\pi r^2} \vec{e}_r$
 $\vec{j} = \vec{D} \times \vec{B} = \frac{Q}{4\pi r^2} \vec{e}_r \times \vec{B}$
 $\vec{l} = \vec{r} \times \vec{j} = \frac{Q}{4\pi r^2} r \vec{e}_r \times (\vec{e}_r \times \vec{B}) = \frac{Q}{4\pi r} (\vec{B} \cos \theta \vec{e}_r - \vec{B})$
 $L_z = \int \vec{l}_z dV = -\frac{QB}{4\pi} \int_0^{\pi} \sin^2 \theta \int_0^{2\pi} d\phi \int_{r_1}^{r_2} dr = -\frac{QB}{5} (r_2^2 - r_1^2)$
 $\omega = -\frac{QB}{3I} (r_2^2 - r_1^2)$